## 232. Molecular Polarisability. The Anisotropy of the $\mathrm{C}=\mathrm{C}$ Bond.

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Molar Kerr constants and dielectric polarisations in carbon tetrachloride at $25^{\circ}$ are recorded for cis- and trans-dichloro-, $1: 1$-dichloro-, trichloro-, and tetrachloro-ethylenes. Molecular anisotropies are also given for the three (of these five) chloroethylenes which are polar. The longitudinal and transverse polarisabilities of the $\mathrm{C}-\mathrm{Cl}$ bond are obtained from carbon tetrachloride and chloroform and used to analyse the polarisability ellipsoid of 1:1-dichloroethylene. Longitudinal, tranverse, and vertical polarisabilities of the $\mathrm{C}=\mathrm{C}$ link are deduced therefrom as $0.28_{0}, 0.07_{3}$, and $0.07_{7} \times 10^{-23}$ c.c., respectively. These values are tested by application to ethylene and its other chloro-derivatives. Agreement between observed and calculated quantities is satisfactory. Available facts show that cis-dichloroethylene is non-planar.

To ascertain the anisotropy of polarisability of the $\mathrm{C}=\mathrm{C}$ bond, we studied molar Kerr constants and other properties of five chlorinated ethylenes, and analysed them with the help of the known structures of these molecules. Among them, the fundamentally important case is vinylidene dichloride, $\mathrm{CH}_{2}=\mathrm{CCl}_{2}$, because in it the resultant dipole moment undoubtedly lies along the $\mathrm{C}=\mathrm{C}$ bond, and thus along one of the principal axes of the molecular ellipsoid. Accordingly the required longitudinal, transverse, and vertical polarisabilities, $b_{\mathrm{L}}{ }^{\mathrm{O}=0}, b_{\mathrm{T}}{ }^{0=0}$, and $b_{\mathrm{V}}{ }^{\mathrm{C}=0}$ respectively, can be calculated; the values so obtained are of general applicability to ethylene and the other substances examined.

## Experimental

Materials.-Carbon tetrachloride, used as solvent throughout, was dried ( $\mathrm{CaCl}_{2}$ ), slowly fractionated ( 1 m . column packed with glass helices), and stored over calcium chloride. The isomeric dichloroethylenes were obtained from a B.D.H. " technical " grade. This, after being dried ( $\mathrm{K}_{2} \mathrm{CO}_{3}$ ), was fractionally distilled under oxygen-free nitrogen in absence of light. The following fractions were collected: trans-dichloroethylene, b. p. $47 \cdot 40^{\circ} \pm 0.005^{\circ} / 757 \cdot 6 \pm 0.05$ $\mathrm{mm} ., n_{\mathrm{D}}{ }^{25}=1 \cdot 44348$; cis-dichloroethylene, b. p. $59 \cdot 85-59 \cdot 90^{\circ} / 759 \cdot 2-760 \cdot 0 \mathrm{~mm} ., n_{\mathrm{D}}{ }^{25}=$ $\mathbf{1} \cdot 44615$. These were sealed and kept in the dark. Trichloro- and tetrachloro-ethylenes were specially prepared and fractionated samples (presented by Imperial Chemical Industries, Australia and New Zealand, Limited, whom we thank) with b. p. and $n_{\mathrm{D}}{ }^{25}$ respectively of 86-4- $86 \cdot 6^{\circ} / 760 \mathrm{~mm}$., $1 \cdot 47503$, and $120-122^{\circ} / 760 \mathrm{~mm}$., $1 \cdot 50328$; they also were preserved out of the light. Vinylidene dichloride was obtained by treatment of $1: 1: 2$-trichloroethane (also presented as above) with lime (cf. Beilstein s " Handbuch," 3rd suppl., Vol. 1, p. 647), b. p. $31 \cdot 4-32 \cdot 0^{\circ} / 760 \mathrm{~mm}$.

Apparatus, Techniques, and Methods of Calculation.-These were as described previously. ${ }^{1-6}$
${ }^{1}$ Le Fèvre and Le Fèvre, J., 1953, 4041; 1954, 1577.
${ }^{2}$ Le Fèvre and Le Fèvre, Rev. Pure Appl. Chem., 1955, 5, 261.
${ }^{3}$ Le Fèvre and Le Fêvre, $J$., 1956, 3549.

* Le Fèvre, " Dipole Moments," Methuen, London, 3rd Edn., 1953, Chap. II.
${ }^{5}$ Buckingham, Chau, Freeman, Le Fèvre, N. Rao, and Tardif, J., 1956, 1405.
- Le Fèvre and P. Rao, J., 1957, 3644; 1958, 1465.

TABLE 1. Depolarisation factors for solutions in carbon tetrachloride.*

| Solute: cis-Dichloroethylene |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $10^{5} f_{2}$ | 3753 | 7379 | 11106 | 14256 | 16969 |
| $10^{2} \Delta_{12}$ | 5.873 | $8 \cdot 370$ | 10.52 | 13.00 | 14.90 |
| Solute: 1:1-Dichloroethylene |  |  |  |  |  |
| $10^{5} f_{3}$ | 1559.5 | 2509 | 3349.5 | 3966 | 5044 |
| $10^{2} \Delta_{12}$ | $5 \cdot 391$ | 6.062 | 6.589 | $6 \cdot 968$ | $7 \cdot 635$ |
| Solute: Trichloroethylene |  |  |  |  |  |
| $10^{5} f_{2}$ | 1592 | 4278 | 6591 | 9378.5 | 11762.5 |
| $10^{2} \Delta_{12}$ | $5 \cdot 246$ | $8 \cdot 175$ | 10.54 | $13 \cdot 12$ | 16.39 |

Table 2. Dielectric constants, densities, refractive indexes, and Kerr constants as functions of weight fractions for solutions in carbon tetrachloride * at $25^{\circ}$.

|  |  |  |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| cis-Dichloroethylene |  |  |  |  |  |  |  |
| $10^{5} w_{2}$ | $\ldots \ldots \ldots \ldots$. | 1225 | 1866 | 2596 | 3082 | 3666 | 4073 |
| $\varepsilon_{12}$ | $\ldots \ldots \ldots \ldots \ldots$. | 2.3059 | 2.3463 | $2 \cdot 3936$ | 2.4249 | $2 \cdot 4626$ | 2.4890 |
| $d_{12}$ | $\ldots \ldots \ldots \ldots \ldots$ | 1.57965 | 1.57719 | 1.57432 | 1.57239 | 1.57038 | 1.56853 |
| $10^{4} \Delta n$ | $\ldots \ldots \ldots \ldots$. | 0 | -2 | -3 | -4 | -5 | -7 |
| $10^{5} w_{2}$ | $\ldots \ldots \ldots \ldots$. | 5810 | 6903 | 7181 | 9213 | 14121 | 16445 |
| $10^{7} \Delta B$ | $\ldots \ldots \ldots \ldots$. | 0.037 | 0.041 | 0.043 | 0.057 | 0.087 | 0.108 |

whence $\Sigma \Delta \varepsilon / \Sigma w_{2}=6.423 ; \Sigma \Delta d / \Sigma w_{2}=-0.3924 ; \Sigma \Delta n / \Sigma w_{\mathrm{g}}=-0.0127 ; \Sigma w_{2} \Delta B / \Sigma w_{2}{ }^{2}=0.630_{6}$.

| trans-Dichloroethylene. |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ${ }^{10}{ }^{5} w_{2}$ | 546 | 1576 | 1603 | 1824 | 3010 | 3655 | 4411 | $4735 \cdot 5$ | 8069 |
| $\varepsilon_{12} \ldots \ldots$. | 2.2268 | 2.2262 | 2.2257 | 2. 2257 | 2.2247 | 2.2246 | 2.2239 | ${ }^{2} 22239$ | - |
| ${ }_{12}^{10^{4}}{ }^{\text {d }}$ | ${ }^{1.58201}$ | 1.57756 -10 | 1.57742 -10 | 1.57652 -10 | ${ }_{\text {1. } 57125}$ | 1.56857 -12 | ${ }_{1}^{1.56544}$ | 1.56497 -15 | 20 |
| $\begin{array}{ll} 10^{5} w_{2} & \ldots \\ 10^{7} \Delta B & \ldots \end{array}$ | $\begin{aligned} & 1107 \\ & 0.011 \end{aligned}$ | $\stackrel{1694 \cdot 5}{0.014}$ | $\begin{aligned} & 3350 \\ & 0.029 \end{aligned}$ | $\begin{aligned} & 3366 \\ & 0.029 \end{aligned}$ | $\begin{aligned} & 4187 \\ & 0.034 \end{aligned}$ | $\begin{aligned} & 8069 \\ & 0.071 \end{aligned}$ |  |  |  |

$$
=0.865_{\mathrm{g}} .
$$



| Tetrachloroethylene |  |  |  |  |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $10^{6} w_{2}$ | $\ldots$ | 802 | 1619 | 2189 | 3167 | 3900 | 4543 | 5351 | 5652 |
| $\varepsilon_{12}$ | $\ldots \ldots$ | 2.2274 | 2.2278 | - | 2.2286 | 2.2290 | 2.2302 | 2.2297 | 2.2301 |
| $d_{12}$ | $\ldots \ldots$ | 1.58477 | 1.58505 | 1.58523 | 1.58542 | 1.58558 | 1.58578 | 1.58596 | 1.58606 |
| $10^{4} \Delta n$ | $\ldots$ | 0 | 5 | 6 | 11 | 14 | 16 | 20 | 21 |
| $10^{5} w_{2}$ | $\ldots$ | 2876 | 3958 | 6462 | 7118 | 10248 | 11748 |  |  |
| $10^{7} \Delta B$ | $\ldots$ | 0.020 | 0.028 | 0.043 | 0.050 | 0.070 | 0.079 |  |  |

whence $\sum \Delta \varepsilon / \sum w_{2}=0.0551 ; \Delta \Sigma d / \sum w_{2}=0.0277 ; ~ \sum \Delta n / \sum w_{2}=0.0342 ; ~ \sum w_{2} \Delta B / \sum w_{2}{ }^{2}=0.681$. $*$ Values for $w_{2}=0, \varepsilon_{1}=2.2270, d_{1}=1.58454, n_{1}=1.4574\left(\mathrm{Na}-\mathrm{d}\right.$ light), $B_{1}=0.070 \times 10^{-7}$ (Na-D light).

Observations are listed in Tables 1-4, wherein symbols have the following meanings: $w_{2}$, weight fraction; $f$, molar fraction; $\Delta$, depolarisation factor; $\varepsilon$, dielectric constant; $d$, density; $n$, refractive index; $B$, Kerr constant; suffixes 1, 2, and 12 denote respectively solvent, solute, and solution; $\Delta \Delta, \Delta \varepsilon, \Delta d$, etc., represent alterations of the property concerned from solvent to solution; $\infty_{\delta_{2}}{ }^{2}$ is the molecular anisotropy at infinite dilution, and is different from $\delta$ in Table 4; $\alpha, \beta, \gamma$, and $\delta$ are coefficients in the equations $\varepsilon_{12}=\varepsilon_{1}\left(1+\alpha w_{2}\right), d_{12}=d_{1}\left(1+\beta w_{2}\right), n_{12}=$ $n_{1}\left(1+\gamma n_{1}\right)$, and $B_{12}=B_{1}\left(1+\delta w_{2}\right) ;{ }_{\infty}\left({ }_{m} K_{2}\right)$ and ${ }_{\infty} P_{2}$ are molar Kerr constants and total dielectric polarisations at infinite dilution; $R_{\mathrm{D}},{ }_{\mathrm{E}} P,{ }_{\mathrm{D}} P$, and $\mu$ indicate molar refractions

Table 3. Molecular anisotropies of solutes at infinite dilution.

| Solute | R.H.S. of equation giving $\Delta \Delta_{12}$ | $D^{*}$ | $10^{3}{ }_{\infty} \delta_{2}{ }^{2}$ |
| :---: | :---: | :---: | :---: |
| cis- $\mathrm{C}_{2} \mathrm{H}_{2} \mathrm{Cl}_{2}$ | $0.6261 f_{2}+0.272 f_{2}{ }^{2}$ | -0.2225 | $31.5{ }_{2}$ |
| 1: $1-\mathrm{C}_{2} \mathrm{H}_{2} \mathrm{Cl}_{2}$ | $0.7165 f_{2}-1.18 f_{2}{ }^{2}$ | $-0.3085$ | 35.71 |
| $\mathrm{C}_{2} \mathrm{HCl}_{3} \ldots$ | $1.048 f_{2}+0.275 f_{2}{ }^{2}$ | $-0.1200$ | $51 \cdot 2_{1}$ |
|  | $D$ is given by $d_{12}=d_{1}+D f_{2}$. |  |  |

Table 4. Calculation of results.

| Solute | $\left(\alpha \varepsilon_{1}\right)_{w_{2}=0}$ | $(\beta)_{w_{2}}=0$ | $\gamma$ | $(\delta)_{w_{2}=0}$ | $10^{12}{ }_{\infty}\left({ }_{m} K_{2}\right)$ | ${ }_{\infty} P_{2}$ (c.c.) | $R_{\text {D }}$ (c.c.) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| cis $-\mathrm{C}_{2} \mathrm{H}_{2} \mathrm{Cl}_{2}$ | $6 \cdot 423$ | $-0.2476$ | $-0.009$ | $9 \cdot 0_{1}$ | $5 \cdot 25$ | $88 \cdot 1{ }_{3}$ | $20.25{ }^{\text {a }}$ |
| trans $-\mathrm{C}_{2} \mathrm{H}_{2} \mathrm{Cl}_{2}$ | $-0.06_{8}$ | $-0.2930$ | $-0.024$ | $12 \cdot 3$ | $9 \cdot 96$ | $22 \cdot 2{ }_{6}$ | $20.60{ }^{\text {a }}$ |
| 1: $1-\mathrm{C}_{2} \mathrm{H}_{2} \mathrm{Cl}_{2} \ldots$ | 2.97 。 | $-0.3008$ | $-0.020$ | 47.49 | 34.42 | $53 \cdot 6{ }_{7}$ | $20.43{ }^{\text {e }}$ |
| $\mathrm{C}_{2} \mathrm{HCl}_{3} \ldots \ldots \ldots$. | $1 \cdot 11_{1}$ | $-0.091{ }^{6}$ | 0.012 | 13.97 | 14.29 | 41.74 | $25 \cdot 42^{\text {\% }}$ |
| $\mathrm{C}_{2} \mathrm{Cl}_{4} \ldots \ldots \ldots \ldots$. | $0.05{ }^{\text {a }}$ | $0.017_{5}$ | $0.023_{5}$ | 9.73 | 13.2 ${ }_{4}$ | 30.82 | $30.33{ }^{\text {h }}$ |
| Solute | ${ }^{P}$ (c.c.) | ${ }_{\mathrm{D}} P$ (c.c.) | $\boldsymbol{\mu}$ (D) | $\begin{gathered} 10^{35}\left(\theta_{1}+\right. \\ \left.\theta_{2}\right) \end{gathered}$ | $\begin{aligned} & { }^{10^{23}\left(b_{1}+\right.} \\ & \left.b_{2}+b_{3}\right) \end{aligned}$ | $\left.10^{48} \sum_{b_{j}}\right)^{2}\left(b_{i}-\right.$ | $10^{35} \theta_{2}$ |
| cis $-\mathrm{C}_{2} \mathrm{H}_{2} \mathrm{Cl}_{2} \ldots$ | $19.62{ }^{\text {b }}$ | $21.6{ }^{\text {c }}$ | 1.80 | $1.24{ }_{8}$ | $2.33{ }_{3}$ | 17-16 | 0.228 |
| trans $-\mathrm{C}_{2} \mathrm{H}_{2} \mathrm{Cl}_{2}$ | $19.92{ }^{\text {b }}$ | $22 \cdot 3{ }^{\text {d }}$ | 0 | $2 \cdot 36{ }_{8}$ | $2 \cdot 36{ }_{9}$ | - | -11 |
| 1: $1-\mathrm{C}_{2} \mathrm{H}_{2} \mathrm{Cl}_{2} \ldots$ | $19.78{ }^{\prime}$ | $21.8{ }^{\text {c }}$ | 1.25 | $8.18{ }_{5}$ | $2 \cdot 35{ }^{\text {a }}$ | 19.75 | 7.011 |
| $\mathrm{C}_{2} \mathrm{HCl}_{3} \ldots \ldots \ldots$. | $24 \cdot 61{ }^{\prime}$ | $27.1{ }^{\text {c }}$ | $0 \cdot 85$ | $3 \cdot 398$ | 2.92 ${ }_{6}$ | $43 \cdot 84$ | $0 \cdot 793$ |
| $\mathrm{C}_{2} \mathrm{Cl}_{4} \ldots \ldots \ldots \ldots$. | $29.81{ }^{\text {n }}$ | $30 \cdot 8{ }^{\text {d }}$ | 0 | 3.149 | 3.545 | - | - |

a Calc. from Timmermans, " Physico-chemical Constants of Pure Organic Compounds," Elsevier, New York and London, 1950, pp. 277/8. "bxtrapolated from $R_{\alpha}$ and $R_{\beta}$ calc. from $a$. "Taken as ${ }_{\mathrm{E}} P \times 1 \cdot 1 .{ }^{\text {d }}$ I.e., ${ }_{\infty} P_{2}$. "From Schildknecht, "Vinyl and Related Polymers," Wiley, New York, 1952, p. 449. S I.e., $0.968 R_{\mathrm{D}}$; cf. ratios $\mathrm{E} P / R_{\mathrm{D}}$ for cis- and trans-isomers. ${ }^{\circ}$ From Beilstein, 3rd Suppl., Vol. 1. ${ }^{h}$ Calc. from refractions listed in Landolt and Börnstein's Tables, 1912 Edn.

Table 5. Semi-axes of polarisability ellipsoids.

|  | $10^{23} b_{1}$ | $10^{23} b_{2}$ | $10^{23} b_{3}$ |
| :---: | :---: | :---: | :---: |
| $\mathrm{CH}_{2}: \mathrm{CCl}_{2}$ | 0.896 | 0.879 | 0.575 |
| cis- $\mathrm{C}_{2} \mathrm{H}_{2} \mathrm{Cl}_{2}$ | 0.7795 | 0.946 | $0 \cdot 608$ |
| $\mathrm{C}_{2} \mathrm{HCl}_{3}$ | 1.003 | 1.231 | 0.692 |

(sodium light), electronic and distortion polarisations, and dipole moments; $b_{1}, b_{2}$, and $b_{3}$ are semi-axes of a molecular polarisability ellipsoid; $\theta_{1}$ and $\theta_{2}$ are explained and expanded in ref. 2.

Molecular Semi-axes from Experiment.-Semi-axes of the polarisability ellipsoids for the three polar solutes are given in Table 5. They have been calculated on the assumption that $\mu_{\text {resultant }}$ in each case is acting parallel to one of the semi-axes; this may not be valid for trichloroethylene although it obviously is so for the other two molecules. Semi-axes for the non-polar compounds cannot, of course, be obtained directly from experiment (see ref. 2, p. 287).

Previous Measurements.-Dielectric polarisation measurements in carbon tetrachloride have been previously recorded only for trichloroethylene, to which a polarity of 0.8 D is ascribed. ${ }^{7}$ Other determinations, either in benzene or "unspecified solvents," are: 1:1-dichloroethylene, ${ }^{8}$ 1.30 or 1.18 D , cis-dichloroethylene, ${ }^{7} 1.74-1.89 \mathrm{D}$, trans-dichloroethylene, ${ }^{7} 0-0.7 \mathrm{D}$, trichloroethylene, ${ }^{7} 0.94 \mathrm{D}$, and tetrachloroethylene, ${ }^{7} 0 \mathrm{D}$. As a vapour the cis-dichloro-compound shows ${ }^{9} \mu=1.90 \pm 0.02 \mathrm{D}$.

Sachsse ${ }^{10}$ has stated, without giving observational details, that cis- and trans-dichloro- and

[^0]tetrachloro-ethylenes in carbon tetrachloride at about $4^{\circ}$ had $_{\mathrm{m}} \mathrm{K}^{\prime} \mathrm{s}$ of $\mathbf{8 . 2}, 8.4$, and $12.8 \times 10^{-12}$ respectively. The electric double refractions noted for the cis- and trans-dihalogeno-substances as gases by Stuart and Volkmann ${ }^{11}$ correspond (according to Sachsse) to ${ }_{\mathrm{m}} \mathrm{K}$ 's of $\mathbf{7 . 5}$ and $18.6 \times 10^{-12}$.

No reference can be found to the depolarisation of light scattered by these five solutes either undiluted or dissolved.

## Discussion

Derivation of Bond Polarisability Ellipsoid for $\mathrm{C}=\mathrm{C}$. - The desired values of $b_{\mathrm{L}}{ }^{0=0}, b_{\mathrm{T}}{ }^{0=0}$, and $b_{\mathrm{V}}{ }^{\mathrm{o}=0}$ can be extracted from the molecular ellipsoid found (Table 5) for 1:1-dichloroethylene, provided that specifications are known for the structure of $\mathrm{CH}_{2}=\mathrm{CCl}_{2}$ and for the polarisability ellipsoids of the $\mathrm{C}-\mathrm{H}$ and $\mathrm{C}-\mathrm{Cl}$ bonds.

The $\mathrm{C}-\mathrm{H}$ link, for reasons given before, ${ }^{2,12}$ is taken as isotropic, i.e., $b_{\mathrm{L}}{ }^{0-\mathrm{H}}=b_{\mathrm{T}}{ }^{0-\mathrm{H}}=$ $b_{\mathrm{V}}^{0-\mathrm{H}}=0.064 \times 10^{-23}$ c.c. Information on $\mathrm{C}-\mathrm{Cl}$ can be obtained from the molecules $\mathrm{CCl}_{4}$ and $\mathrm{CHCl}_{3}$. For the former, ${ }^{18} b_{1}=b_{2}=b_{3}=1.026 \times 10^{-23}$ and for the latter $b_{1}=0.673 \times 10^{-23}$ c.c. According to Allen and Sutton's list, ${ }^{14}$ the $\mathrm{Cl}-\mathrm{C}-\mathrm{Cl}$ angles in $\mathrm{CCl}_{4}$ and $\mathrm{CHCl}_{3}$ are tetrahedral and $112^{\circ}$ respectively, whence $b_{\mathrm{L}}{ }^{-0}=0.399 \times 10^{-23}$ and $b_{\mathrm{T}}{ }^{\mathrm{O}-\mathrm{Cl}}=0.185 \times 10^{-23}$ c.c. From ref. 14 the configuration of $\mathrm{CH}_{2}=\mathrm{CCl}_{2}$ is set by a $\mathrm{Cl}-\mathrm{C}-\mathrm{C}$ angle of $122^{\circ} \pm 1^{\circ}$. The above facts, together with the appropriate trigonometrical quantities, lead to the equations for $\mathrm{CH}_{2}: \mathrm{CCl}_{2}: 10^{23} b_{1}=0.618+b_{\mathrm{L}}{ }^{\mathrm{c}=0} ; 10^{23} b_{2}=0.806+$ $b_{\mathrm{T}}{ }^{\mathrm{O}=0}$; and $10^{23} b_{3}=0.498+b_{\mathrm{V}}{ }^{0}=0$, from which, in turn, the bond semi-axes emerge as: $10^{23} b_{\mathrm{L}}{ }^{0}=\mathrm{C}=0.280$ c.c. ; $10^{23} b_{\mathrm{T}} \mathrm{C}=0=0.073$ c.c.; and $10^{23} b_{\mathrm{V}}{ }^{\mathrm{C}=0}=0.077$ c.c.

This is actually the second estimate of the anisotropy of polarisability of the $\mathrm{C}=\mathrm{C}$ bond to be made completely from experiment, Sachsse ${ }^{10}$ having reported $0.392,0.094$, and $0.035 \times 10^{-23}$ for the three $b^{0=0}$ 's in question. Since Sachsse depended upon the then available intervalency angles for calculation from his ${ }_{m} K$ 's (see above), we consider the present to be the more reliable. Wang ${ }^{15}$ and Denbigh ${ }^{16}$ quote values of 0.302 and $0.286 \times$ $10^{-23}$ for $b_{\mathrm{L}}{ }^{0}=0$ but appear to have used the Kerr constant given in the literature for ethylene and assumed, without a priori justification, that $b_{\mathrm{T}}{ }^{0}=0=b_{\mathrm{V}}{ }^{0}=0$. Bolton ${ }^{17}$ and Mueller, ${ }^{18}$ by different theoretical routes, have deduced that $b_{L} \alpha=0=0.286$ or $0.312 \times$ $10^{-23}$ c.c., respectively. An empirical connection with bond lengths ${ }^{19}$ forecasts $b_{\mathrm{L}}{ }^{\mathrm{O}=0}=$ $0.275 \times 10^{-23}$.

Derivation of Molecular Ellipsoids of Non-polar Chloroethylenes.-Allen and Sutton ${ }^{14}$ give intercentre distances and angles as follows: trans $-\mathrm{C}_{2} \mathrm{H}_{2} \mathrm{Cl}_{2}, \mathrm{C}-\mathrm{Cl} 1.69 \pm 0.03 \AA$, $\mathrm{Cl}-\mathrm{Cl} 4.7 \AA, \mathrm{C}-\mathrm{C}-\mathrm{Cl}$ angle $122.5^{\circ} \pm 1^{\circ} ; \mathrm{C}_{2} \mathrm{Cl}_{4}, \mathrm{C}-\mathrm{C} 1.38$ or 1.34 , both $\pm 0.05 \AA, \mathrm{C}-\mathrm{Cl} 1.71$ or 1.73 , both $\pm 0.02 \AA, \mathrm{C}-\mathrm{C}-\mathrm{Cl}$ angle $122 \cdot 2^{\circ}$ or $123.7^{\circ}$, both $\pm 1^{\circ}$. Taking for the former molecule a double bond length as in $\mathrm{C}_{2} \mathrm{Cl}_{4}$, we predict the semi-axes: $10^{23} b_{1}=1.082$, $10^{23} b_{2}=0.693$, and $10^{23} b_{3}=0.575$ ( $b_{1}$ lying through the $\mathrm{Cl} \ldots \mathrm{Cl}$ centres); ${ }_{\mathrm{m}} K$ (calc.) is therefore $10.7 \times 10^{-12}$ against $10.0 \times 10^{-12}$ found. Improved agreement can be secured by appropriate variations of lengths and angles within the limits stated in ref. 14. If $\mathrm{C}-\mathrm{Cl}$ is kept at $1.69 \AA$, but the angle $\mathrm{C}-\mathrm{C}-\mathrm{Cl}$ is put equal to $120^{\circ}{ }_{\mathrm{m}} \mathrm{K}$ calc. becomes $9.8 \times$ $10^{-12}$.

For tetrachloroethylene it is assumed that the double bond lies along the principal axis $b_{1}$. With the $\mathrm{Cl}-\mathrm{C}-\mathrm{C}$ angle at $122.0^{\circ}$, the polarisability semi-axes are $10^{23} b_{1}=1 \cdot 262$, $10^{23} b=1.426$, and $10^{23} b_{3}=0.817$, or with the angle at $123.7^{\circ}$ they are $10^{23} b_{1}=1.284$, $10^{23} b_{2}=1 \cdot 405$, and $10^{23} b_{3}=0.817$. The ${ }_{m} K$ 's computed for the two sets are $14.0 \times 10^{-12}$ or $13.6 \times 10^{-12}$ respectively, the " found " value being $13.2 \times 10^{-12}$.
${ }_{11}$ Stuart and Volkmann, Ann. Phys., 1933, 18, 121.
12 Le Fèvre and Le Fèvre, Chem. and Ind., 1955, 1121.
13 Armstrong, Aroney, Le Fèvre, Le Fèvre, and Smith, J., 1958, 1474.
14 Allen and Sutton, Aeta Cyyst., 1950, 3, 46.
${ }^{15}$ Wang, J. Chem. Phys., 1939, 7, 1012.
16 Denbigh, Trans. Faraday Soc., 1940, 36, 936.
${ }^{17}$ Bolton, Trans. Faraday Soc., 1954, 50, 1261.
${ }^{18}$ Mueller, J. Chem. Phys., 1954, 22, 180.
${ }^{10}$ Le Fèvre, Proc. Chem. Soc., 1958, 283.

Prediction of Molar Kerr Constant of Ethylene.-The calculated semi-axes for this molecule are $0.536,0.329$, and $0.333 \times 10^{-23}$, whence $\left(b_{1}-b_{2}\right)^{2}+\left(b_{2}-b_{3}\right)^{2}+\left(b_{3}-b_{1}\right)^{2}=$ $0.084 \times 10^{-46} ;{ }_{\mathrm{m}} K$ is therefore $1.9_{1} \times 10^{-12}$, or, if the distortion and electronic polarisations recorded by Watson and Ramaswamy ${ }^{20}$ are introduced, $1 \cdot 9_{8} \times 10^{-12}$. Two determinations of $B_{\text {etbylene }}$ are available: $0 \cdot 19_{6} \times 10^{-10}$ at $20^{\circ} / 1 \mathrm{~atm}$., and $\lambda=5460 \AA$, by Kuss, ${ }^{21}$ or $0 \cdot 16_{3} \times 10^{-10}$ at $0^{\circ}, 1 \mathrm{~atm}$., and $\lambda=6500 \AA$, by Breazeale; ${ }^{22}$ these correspond to ${ }_{\mathrm{m}} K^{\prime}$ 's of $1.9_{1}$ or $1.8 \times 10^{-12}$. Considering that the quoted $B$ 's are both extrapolated from observations taken at pressures considerably above normal, we cannot expect better agreement between ${ }_{\mathrm{m}} K_{\text {obs }}$ and ${ }_{\mathrm{m}} K_{\text {calc. }}$.

Applicability of Bond Polarisabilities to Trichloroethylene.-Interpretation of data for this case is difficult because the direction of action of the resultant dipole moment is not known exactly. $\alpha$ is $114^{\circ}$ and $\beta$ is $123^{\circ}$ in (I). ${ }^{14}$ It is highly probable that the axis of


(II)

(III)
maximum polarisability lies parallel to the bonds holding Cl atoms B and C . On such a basis the semi-axes calculable a priori would be: $10^{23} b_{1}=1 \cdot 01_{6}, 10^{23} b_{2}=1 \cdot 21_{7}, 10^{23} b_{3}=$ $0 \cdot 69_{6}$. In deducing $b_{1}, b_{2}$, and $b_{3}$ from experiment (Table 5), the assumption was made that $\mu_{\text {resultant }}$ acts along one of the principal polarisability axes. Because of the smallness of $\mu_{\text {resultant }}, v i z ., 0.85 \mathrm{D}$, the predicted and found $b$ 's should be compared to two significant figures only; when this is done, both sets become $1 \cdot 0,1 \cdot 2$, and $0.7 \times 10^{-23}$. Other dispositions of $b_{\text {maximum }}$ were tried, but each resulted in a larger value for $b_{1 \text { calc. }}$. The implication therefore is that $\mu_{\text {resultant }}$ is acting along a line situated some $24^{\circ}$ anticlockwise from the bond holding atom A ; this seems reasonable.

Conformation of cis-1 : 2-Dichloroethylene.-The structure is specified in ref. 14 as (II). If the molecule is planar, the $\mathrm{Cl}-\mathrm{Cl}$ distance $(3.7 \AA$ ) and the $\mathrm{C}-\mathrm{Cl}$ distance ( $1.67 \AA$ ) quoted (from $X$-ray diffraction on the gas) are not reconcilable with a $\mathrm{Cl}-\mathrm{C}=\mathrm{C}$ angle ( $\alpha$ ) of $\mathbf{1 2 3 \cdot 5}{ }^{\circ}$, it necessitates either ( $a$ ) an abnormally ${ }^{14,23}$ long $\mathrm{C}=\mathrm{C}$ bond (ca. $1 \cdot 8 \AA$ ), or (b) a $\mathrm{Cl}-\mathrm{C}=\mathrm{C}$ angle of $135^{\circ}$. The semi-axes predicted for these two angles are: $b_{1}=0.869, b_{2}=0.908$, $b_{3}=0.575 \times 10^{-23}$ (for $\angle \mathrm{Cl}-\mathrm{C}=\mathrm{C}=123.5^{\circ}$ ), $b_{1}=0.785, b_{2}=0.992, b_{3}=0.575 \times 10^{-23}$ (for $\angle \mathrm{Cl}-\mathrm{C}=\mathrm{C}=135^{\circ}$ ) against values from experiment of $0.779_{5}, 0.946$, and $0.608 \times 10^{-23}$, with which neither set is in good agreement. No variation about $3 \cdot 7 \AA$ is cited for the $\mathrm{Cl}-\mathrm{Cl}$ separation but the likelihood of considerable error is diminished by the fact that the corresponding length (given as $4.7 \AA$ ) in the trans-isomer is close to that calculated ( $4.6 \AA$ ) from the appropriate molecular dimensions.

Accordingly non-planar models have been considered (III). Taking the $\mathrm{C}=\mathrm{C}$ distance as $1.34 \AA$ and that for $\mathrm{C}-\mathrm{Cl}$ as $1.67 \AA$, we can evaluate an angle $\theta$ by geometry as $34^{\circ} 23^{\prime}$; $\alpha$ is $123.5^{\circ} ; \theta$ is the angle of projection of each $\mathrm{C}-\mathrm{Cl}$ bond on the plane which contains the long axis of the double bond and is symmetrically between the two planes in which the two $\mathrm{Cl}-\mathrm{C}=\mathrm{C}$ triangles are lying; $b_{1}$ also must be situated in this plane, and the $\mathrm{C}-\mathrm{Cl}$ moments will act at an angle $\rho$ to $b_{1}$ (where $\rho=52^{\circ} 13^{\prime}$ ). These data being used, $b_{1}$ (calc.) becomes $0.732 \times 10^{-23}$, while $b_{1}$ (expt.) $=0.779_{5} \times 10^{-23}$. Bearing in mind the fact that $b_{1}$ (calc.) is based on two different bond lengths, one atom-atom distance, and one electron-diffraction angle determination, we can accept the agreement reached.

Alternatively, more precise information on the angles $\theta, \phi$, and $\rho$ can be obtainable from the measured quantity $b_{1}$, because there can be no doubt where $b_{1}$ lies with reference to the
${ }^{20}$ Watson and Ramaswamy, Proc. Roy. Soc., 1936, $A, 156,144$.
${ }^{21}$ Kuss, "Elektro-optischer Kerreffekt bei hohen Drucken im Übergangsgebiet Gasförmig-flüssig," Berlin, 1940.
${ }_{22}$ Breazeale, Phys. Rev., 1936, 49, 625.
${ }^{23}$ Stuart, "Die Struktur des Freien Moleküls," Springer, Berlin, 1952, pp. 162 and 172.
$\mathrm{C}=\mathrm{C}$ and the $\mathrm{C}-\mathrm{Cl}$ links. If we write $b_{1}=2 b_{\mathrm{L}}{ }^{0-0 l} \cos ^{2} \rho+2 b_{\mathrm{T}}{ }^{0-0 l} \sin ^{2} \rho+b_{\mathrm{T}}{ }^{0}=0+2 b_{\mathrm{L}} \mathrm{O}-\mathrm{H}$, where $b_{1}=0.779_{5} \times 10^{-23}$, we obtain $\rho$ as $45^{\circ} 44^{\prime}, \theta$ as $27^{\circ} 81^{\prime}$, and $\phi$ as $51^{\circ} 40^{\prime}$, while the azimuthal angle between the planes of the $\mathrm{C}=\mathrm{C}-\mathrm{Cl}$ units is $66^{\circ} 20^{\prime}$. That these angles are more suitable than those deduced by geometry can be seen from the facts that they lead to a $\mathrm{Cl}-\mathrm{Cl}$ separation of $3.5_{3} \AA$ (against $3.7 \AA$ reported ${ }^{14}$ ) and a $b_{2}$ calc. of $0.947 \times 10^{-23}$ (against $0.946 \times 10^{-23}$ found); $b_{2}$ is assumed to be situated parallel to the $\mathrm{Cl}-\mathrm{Cl}$ direction. By difference (Table 4), $b_{3}$ is $0.606_{5} \times 10^{-23}$ (against $0.608 \times 10^{-23}$ found).

Further Reference to Tri- and Tetra-chloroethylenes.-One might suspect that if cisdichloroethylene is non-planar, the tri- and tetra-chloro-derivatives would be so also, volume factors being presumably responsible. It is therefore relevant to mention that application of the bond lengths and angles listed by Allen and Sutton ${ }^{14}$ to planar configurations of these molecules reveals permitted maximum $\mathrm{Cl}-\mathrm{Cl}$ separations as follow : $3 \cdot 1_{8} \AA$ for cis-dichloroethylene, $3 \cdot 2_{4} \AA$ for trichloroethylene, and $3 \cdot 60 \AA$ for tetrachloroethylene. Since the minimum effective radius of combined chlorine is ca. $1 \cdot 6 \AA$ (Stuart ${ }^{24}$ quotes it as $1 \cdot 58 \AA$ ), there can be no objection to the assumption of flatness for the tri- and tetra-chloro-substances. Even so, the degree of non-planarity now inferred for cisdichloroethylene appears excessive if steric causes are alone operative, and no satisfactory alternative explanation suggests itself. The same remarks could be made concerning Bastiansen and Hassel's conclusions ${ }^{25}$ that in $o$-dichloro- and hexachloro-benzenes the halogens are bent out of the plane of the ring by $18^{\circ}$ and $12^{\circ}$ respectively.

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${ }_{24}$ Stuart, Z. phys. Chem., 1935, B, 27, 350.
${ }^{25}$ Bastiansen and Hassel, Acta Chem. Scand., 1947, 1, 489.


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    ${ }^{8}$ Rogers, J. Amer. Chem. Soc., 1947, 69, 1243; Errera, Physikal. Z., 1926, 27, 764.

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    ${ }^{10}$ Sachsse, Physikal. Z., 1935, 36, 357.

